

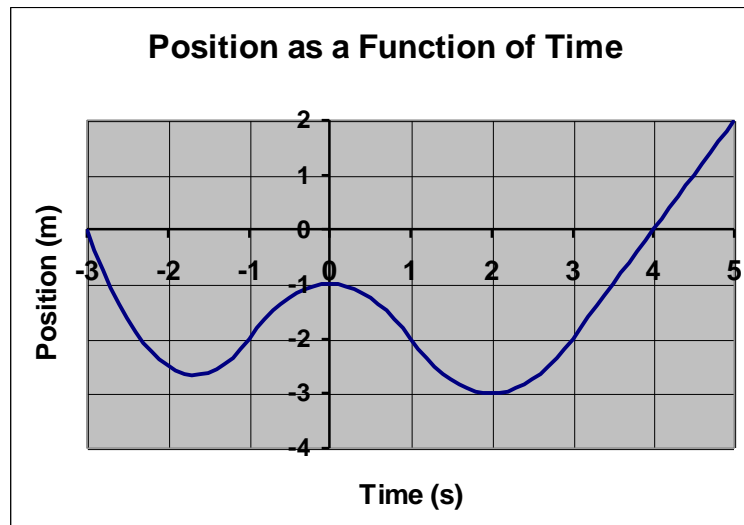
## Quiz #2: Physics 201

NAME: SOLUTIONS

Do **YOUR OWN WORK** and **SHOW ALL OF IT!** (Continue on back, clearly labeled, if necessary)

This quiz does NOT require the use of a calculator. You may write answers as algebraic expressions (that is, write that  $x = 33.7$  and  $y = 108.4$ , and that the answer is  $(x/y)$  kg m/s<sup>2</sup>). Trig functions and square roots may be left in that form if you do not know the results (that is  $\sin 25^\circ$  or  $\sqrt{30}$ ).

All answers **MUST** include appropriate **units and dimensions**.



1. The graph above shows a plot of the position (in meters) of a toy car as a function of time (in seconds) during an eight second period. Answer all of the questions below that you can using the information in the graph, **and always explain your reasoning**. If you think you need more information to answer a question, please explain what else you need to know.
  - a) When, if ever, during that eight second period was the velocity of the car zero? Indicate all times or time intervals between  $t = -3$  s and  $t = 5$  s, and explain your reasoning.

At about  $t = -1.7$  s and  $t = 0.0$  s and  $t = 2.0$  s.  
*This is when the slope of the graph (or the slope of a tangent line) is zero.*
  - b) When, if ever, during that eight second period was the velocity of the car positive? Indicate all times or time intervals between  $t = -3$  s and  $t = 5$  s, and explain your reasoning.

During  $[-1.7$  s <  $t$  <  $0.0$  s] and  $[2.0$  s <  $t \leq 5.0$  s]  
*This is when the slope of the graph (or the slope of a tangent line) is positive.*

*See next page!*

- c) When, if ever, during that eight second period was the velocity of the car constant? Indicate all times or time intervals between  $t = -3 \text{ s}$  and  $t = 5 \text{ s}$ , and explain your reasoning.

During  $[3.0 \text{ s} < t \leq 5.0 \text{ s}]$

*This is when the graph is a straight line, so the slope of the graph is constant.*

- d) When, if ever, was the acceleration of the car positive. List all times or time intervals between  $t = -3 \text{ s}$  and  $t = 5 \text{ s}$ , and explain your reasoning.

During  $[-3.0 \text{ s} \leq t < -1.0 \text{ s}]$  and  $[1.0 \text{ s} < t < 3.0 \text{ s}]$

*This is when the graph curves upward, so the slope of the graph is increasing.*

- e) When, if ever, was the speed of the car increasing? List all times or time intervals between  $t = -3 \text{ s}$  and  $t = 5 \text{ s}$ , and explain your reasoning.

During  $[-1.7 \text{ s} \leq t < -1.0 \text{ s}]$  and  $[0.0 \text{ s} \leq t < 1.0 \text{ s}]$  and  $[2.0 \text{ s} < t < 3.0 \text{ s}]$

*This is when the slope of the graph is getting **farther from zero** (either + or -).*

- f) If you were to plot the *velocity* of the car using the same choice of coordinates that was used to make the position plot above, at what time(s) would the **velocity** be a maximum? (remember:  $0 > -1$ ; “zero” is greater than “negative one”.) Explain your reasoning.

*As far as we can tell, this is true at  $t = -1.0 \text{ s}$  and  $[3.0 \text{ s} < t \leq 5.0 \text{ s}]$ . *This is when the slope of the graph is greatest which turns out to be  $2.0 \text{ m/s}$ .**

- g) Estimate the velocity of the car when  $t = 1 \text{ s}$ . (Don't just guess! Show your work!)

There is some estimation and artistic judgement here, but if I draw a tangent line it appears to have a slope of  $-2.0 \text{ m/s}$ .

- h) Estimate the average acceleration between times  $t = 2 \text{ s}$  and  $t = 3 \text{ s}$ . (Show your work.)

One has to draw two tangent lines for this part, but they are easy. When  $t = 2 \text{ s}$  the graph is horizontal so the velocity is zero. When  $t = 3 \text{ s}$  the graph is beginning a long straight phase with a constant slope of  $+2.0 \text{ m/s}$ . So the average acceleration is

$$\frac{(+2.0 \text{ m/s}) - (0.0 \text{ m/s})}{3.0 \text{ s} - 2.0 \text{ s}} = +2.0 \text{ m/s}^2$$

- i) Estimate the average acceleration between times  $t = -2 \text{ s}$  and  $t = 3 \text{ s}$ . (Show your work.)

We get to reuse what we know about  $t = 3 \text{ s}$  (the slope is  $+2.0 \text{ m/s}$ ). When  $t = -2 \text{ s}$  the graph has a slope of  $-1.0 \text{ m/s}$ . So the average acceleration is

$$\frac{(2.0 \text{ m/s}) - (-1.0 \text{ m/s})}{3.0 \text{ s} - (-2.0 \text{ s})} = +0.6 \text{ m/s}^2$$